Abstract

Long-term contracts have long dominated the international market for LNG. Since 2000, however, the proportion of LNG-traded spot or under short-term contracts has grown substantially, while long-term contracts have become more flexible. While long-term contracts increase the debt capacity of large, long-lived, capital investments by reducing cash flow variability, they also may limit the ability of the contracting parties to take advantage of profitable ephemeral trading opportunities. After developing a model that illustrates these trade-offs, we argue that increased LNG market liquidity resulting from a number of exogenous changes is likely to encourage much greater volume and destination flexibility in contracts and increased reliance on short-term and spot market trades. These changes would, in turn, reinforce the initial increase in market liquidity.

Keywords: Long-term contracts, LNG, investment project leverage, opportunistic trades
1. Introduction

Traditionally, LNG was almost exclusively traded under inflexible long-term contracts. Since 2000, however, the proportion of LNG traded spot or on contracts of less than four years duration has risen substantially. In addition, as emphasized by Weems (2006), long-term LNG contracts have become more flexible. For example, recent contracts allow quantity adjustments under more contingencies, greater destination flexibility, and a wider range of pricing options (including linking LNG prices to spot market natural gas prices) and price review provisions. Such contract provisions allow parties not only to cope with temporary operational disruptions but also to exploit profitable short-term trading opportunities.

This paper develops a model of the costs and benefits of an optimal long-term LNG contract, defined as a contract giving the largest combined expected net present value to the trading partners. We then analyze how increased spot market liquidity, reflected in changes such as increased ability to trade without adversely affecting prices, reduced price variability, and smaller gaps between buying and selling prices, affects such optimal contracts. We find that the net benefits of a long-term contract for parties establishing new LNG projects declines, while partners in existing long-term contracts can reap greater benefits from participating in spot markets. Adjusting contract terms to allow firms to exploit these opportunities will further increase spot market liquidity.

We conclude that the proportion of LNG traded on long-term contracts is likely to further decline. Even if most LNG trade continues to be covered by long-term contracts, such contracts are likely to continue evolving toward offering much greater volume and destination flexibility.
2. Some recent developments in LNG markets

Figure 1, based on data from the International Group of Liquefied Natural Gas Importers (GIIGNL), shows that spot and short-term (less than four-year duration) contract trades generally increased from 2000 to more than 25% of total trade in 2011. Furthermore, since contracted volume plus spot and short-term trade exceeded actual trade every year since 2001 in both basins, parties to long-term contracts evidently engaged in spot and short-term trade. The model we develop later will allow for such short-term trades.

Writing in the IGU 2006-2009 Triennium Work Report (International Gas Union (2009), hereafter IGU (2009)), Lange notes that the first swaps were arranged to save transportation costs or satisfy ephemeral peak demands. Surplus volumes from temporary demand reductions were also sold into US terminals, which acted as a sink for the global LNG market. In the five years before he wrote, however, traders seeking to profit from arbitrage opportunities increasingly dominated the market.

Park, also writing in IGU (2009), remarked that the then recently signed contract between Malaysian LNG (Tiga) and three Japanese customers allowed for 40% volume flexibility instead of the 5–10% in a conventional contract. Nakamura (also in IGU (2009)) noted that some then recent LNG export projects had made final investment decisions without 100% off-take commitments by buyers, leaving uncommitted quantities for spot market trades. Nakamura also discussed growth in “Branded LNG,” where non-consuming buyers purchase LNG from multiple projects and sell to buyers under their own names. Similarly, Thompson (2009) notes that BG has signed contracts with several suppliers allowing diversion of LNG to higher-value markets. It will use its own ships and storage capacity in Louisiana and Wales to support the activity. Other major liquefaction and regasification terminals have substantial on-site LNG storage. National
Grid sells capacity in a dedicated LNG storage facility at Avonmouth in the UK, while Singapore LNG Corporation has built a regasification terminal with throughput capacity surplus to domestic needs and a goal of pursuing arbitrage opportunities in the LNG market.

Thompson (2009) also notes that expiration of some early long-term LNG contracts has left suppliers with spare capacity but without a need to finance large investments. Some of these suppliers have entered the short-term and spot market rather than sign new long-term contracts.

Figure 1 also reveals that long-term contracted volume exceeded actual trade every year from 2003 in the Atlantic basin. Conversely, actual trade exceeded long-term contracted trade in the Pacific basin in most years. Trade from the Atlantic to the Pacific basin may reflect, in part, the progressive elimination of destination clauses in long-term contracts for LNG supply to the European Union (EU). These clauses forbid buyers from re-selling the product to a different destination, allowing a monopolist to earn more revenue through price discrimination. The EU Commission found them to be anti-competitive in 2001. The elimination of such clauses allowed spot cargoes to respond to the higher economic growth in East Asia than in Europe.

Figure 2, based on data from the Energy Information Administration (EIA), suggests a second reason for the shift of LNG from the Atlantic to the Pacific basin, especially from 2008. US monthly LNG imports jumped from mid-2003 through to the end of 2007. The decline from September 2007 largely reflects increased US and Canadian shale gas production.¹ Firms that had been preparing to export LNG to the US found themselves in need of an alternative market when US imports did not increase as anticipated.

¹ A referee suggested that another factor may have been a decline in demand due to the economic downturn and some warmer than normal winters. However, while data on natural gas marketed production shows some stagnation or decline in demand from September 2008 through February 2010, demand has grown strongly since then.
The Fukushima nuclear disaster in Japan in March 2011 also attracted LNG to the Pacific from the Atlantic basin in 2011 and 2012. Following the disaster, the Japanese government shut down all of Japan’s nuclear power plants, greatly increasing the demand for LNG to generate electricity. Thus Qatar, for example, which had prepared to be a major supplier to the US market, became instead a major spot and short-term LNG supplier to Japan in 2011 and 2012.

North American prices have become so low relative to European and especially Asian prices that, as of December 2012, ten LNG export facilities have been proposed in the US or Canada, with nine more identified as potential sites. Most of these projects would involve import and export facilities at the same location with pipeline connections to the extremely liquid North American natural gas market. These sites would allow short-term diversions or supplementations of LNG shipments on short notice, and without much affecting prices.

In a 20-year contract signed in 2012 by Kogas and Cheniere Energy, the developer of the Sabine Pass liquefaction terminal, Kogas agreed to pay Cheniere a $3.00/MMBTU liquefaction fee while paying 115% of the Nymex Henry Hub price for feed gas sourced from the US natural gas pipeline system. Cheniere reportedly agreed to very similar pricing terms with the Indian state transmission system operator GAIL on the project’s fourth train. Similarly, the developers of the proposed Freeport LNG export plant have signed a liquefaction tolling agreement with BP, who will add the LNG to their worldwide portfolio. Shell is also proposing to add LNG from an export terminal it and Kinder Morgan are planning for Elba Island to its global portfolio rather

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2 According to EIA data, Japanese nuclear output declined more than 43.6% in 2011 relative to 2010, and a further almost 89% in 2012 relative to 2011. While electricity consumption fell more than 7% from 2010 to 2011, it was virtually unchanged from 2011 to 2012. Natural gas consumption jumped more than 13% from 2010 to 2011 and more than an additional 0.5% from 2011 to 2012. The additional compensation for lost nuclear output from 2011 to 2012 came largely from an increase of more than 5.5% in both coal and oil consumption.

3 The liquid UK market (facilitated in the future by trading hubs in continental Europe) also promotes gas on gas competition and similarly contributes to increased LNG market liquidity.
than supplying it to any particular customer. The Elba Island terminal, like one proposed for Lake Charles, is planning to use modular liquefaction units with lower capacity, but also much lower capital costs per unit of capacity than current technology. This should also increase flexibility to respond to market conditions.

Hirschhausen and Neumann (2008) and Ruester (2009) present formal statistical analyses of factors affecting long-term natural gas contract duration. Hirschhausen and Neumann examined 311 long-term contracts between natural gas producers and consumers or traders between 1964 and 2006 (122 contracts covering delivery by pipeline and 189 by transport of LNG). They find that contract duration is shorter for deliveries to the US and UK, and to the EU after the 1998 restructuring directive. Contracts related to investments in specific projects are also significantly longer than other more general contracts. Conversely, contract extensions or renegotiations, which tend not to be linked to specific new investments, are significantly shorter in duration. Contracts signed by new market entrants were also shorter than those signed by incumbents. Contracts covering a larger volume of trade tended to be significantly longer in term.

Ruester (2009) studied 261 long-term (exceeding three years in duration) LNG contracts including more than 80% of long-term LNG supply contracts ever written. The average length for contracts beginning delivery from 2000 was 16.7 years compared to 20.3 years for contracts beginning delivery prior to 2000. Consistent with this, an indicator variable in the regression analysis for contracts beginning delivery from 2000 has a significantly negative effect on duration. Contracts covering a larger share of a regasification terminal’s capacity (indicating the asset is more tied to the relationship) are of significantly longer duration. Measuring risk by the standard deviation of the WTI oil price in the year before the contract was signed, she finds weak

\[4 \text{ After eliminating some contracts with missing data for some variables, she analyzed 224 contracts.}\]
evidence that greater risk reduces contract duration. She also finds a statistically significant negative effect on contract duration of three variables measuring repeated interaction between the contracting parties (each variable tested separately). The variables were the cumulative number of times the same parties had negotiated a contract, the cumulative number of years of bilateral trade between them, and an indicator variable for whether the contract was a renewal. She interprets this result as confirming a hypothesis that lower contracting costs and enhanced reputation reduce the risks that a trading partner will behave opportunistically once investments are sunk. However, as Hirschhausen and Neumann (2008) and Thompson (2009) observed, follow-on contracts may involve smaller investments than new trading relationships. The lesser need for financing may allow parties to take on extra risk by retaining more output for spot market trades. Finally, Ruester confirms the finding of Hirschhausen and Neumann that contracts covering deliveries to more competitive markets are of shorter duration.

3. Related theoretical literature

This paper builds on an extensive literature, mostly based on the Williamson (1979) transaction-cost framework, modeling the benefits of long-term contracts. Williamson views a long-term contractual relationship as intermediate between spot market transactions and vertical integration of buyer and seller.

As Creti and Villeneuve (2005) emphasize in their literature survey, Williamson’s key insight is that a party making durable transaction-specific investments is exposed to ex-post opportunistic

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5 The variable is not statistically significantly different from zero in some regressions and only significant at the 10% level in the remaining ones. She interprets the negative sign as reflecting an aversion to “being bound by an agreement that no longer reflects the actual price level.” By contrast, the risk we consider later in this paper relates to price variations that leave mean prices unchanged.
behavior and strategic bargaining by its trading partner. Long-term contracts limit the opportunities for such behavior.

Creti and Villeneuve also emphasize that the frequency of recurring transactions and uncertainty about future demand and supply conditions affect the value of long-term contracts. In particular, fixing the terms of trade can result in inefficient future trades as supply and demand fluctuate. To mitigate this problem, the contracts allow adjustments that nevertheless are limited in scope to minimize subsequent misinterpretation, dispute and costly adjudication. As Williamson (1979) observes in this regard, while quantity adjustments leave the other party with alternative avenues for making up lost profits, price adjustments are zero-sum.

Take-or-pay clauses are the most common adjustment mechanism in long-term natural gas contracts.6 These allow the buyer to unilaterally decide to take less than the contracted volume in return for compensating the seller for the supply that was not taken. Since the decision is unilateral, such options do not require costly verification of exogenous events.

Creti and Villeneuve discuss a paper by Masten and Crocker (1985) that shows that take-or-pay provisions can yield an efficient ex-post outcome. Masten and Crocker assume that the value \( v(\theta) \) of the contracted volume to the buyer depends on a random demand shock \( \theta \), while the contracted payment to the seller is \( y \). Hence, the buyer would not want to take delivery if \( v(\theta) < y \). Since the value of the trade between the buyer and seller normally exceeds the next best alternative, Masten and Crocker assume that the value \( s \) of the next best alternative for the seller is less than the contracted payment \( y \). If \( v(\theta) < s \), it would be efficient for the buyer to not take the output. But the buyer also would not want to take the output if \( s < v(\theta) < y \), even though

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6 Weems (2006) notes that these were not present in all LNG contracts signed in the 1960s but became standard in LNG contracts signed in the 1970s. He also observes that take-or-pay provisions remain in recent contracts even though they have allowed more flexibility on other margins.
honoring the contract would be efficient. If the buyer has to pay a penalty \( \delta = y-s \) whenever the contracted output is not taken, however, then the contracted output would be refused only when it is efficient to do so.

To implement the efficient take-or-pay rule, the value \( s \) of the next best alternative for the seller must be known to both parties. As Masten and Crocker observe, this could be a reasonable assumption regarding the market price for the gas not taken. More generally, the efficient allocation will depend on shocks affecting both supply and demand in addition to market prices. Some shocks to supply and demand are likely to be private information that cannot be credibly conveyed to the trading partner, or observed by a third party without incurring a cost.

In the model of a long-term contract examined in this paper, the take-or-pay compensation will be a function of publicly observable prices but will not depend on privately observable demand and supply shocks. While the contract generally will not result in ex-post efficient allocations, we show that the inefficiencies are small.

Canes and Norman (1984) also discuss long-term contracts with take-or-pay clauses. Like Masten and Crocker, they point out that a long-term contract protects investors in large facilities with limited alternative uses against later opportunistic behavior by their trading partners. Canes and Norman also observe that such protection comes at the cost of ex-post inefficient allocations, but take-or-pay provisions can accommodate random demand fluctuations. Although they commented that such provisions thereby “reduce cost of contracting and contribute to the efficient production and utilization of natural gas,” they emphasized risk sharing rather than ex-post allocative efficiency. Specifically, they argued that the risk sharing inherent in a long-term take-or-pay contract provides a more predictable cash flow for both producers and buyers, which
in turn facilitates financing of their investments with long-term debt. Industry participants often cite similar concerns as the main motivation for long-term contracts.\(^7\)

The benefits from risk sharing will be reflected in our model of a long-term contract. We show that a major advantage of a long-term contract is that it allows both the seller and the buyer of LNG to finance their investments with more debt.

Our paper also complements analyses, such as Brito and Hartley (2007), that focus on how changes in the surplus generated by different LNG trading arrangements can affect equilibrium market structure when firms can either use long-term contracts or trade in spot markets.

Specifically, Brito and Hartley (2007) examine a world where matches can generate high or low surplus. Firms need to invest \(K\) in infrastructure before a match can generate returns. Firms that have already invested can search in a market for short-term trades, while firms that have yet to invest can search only in a separate, less liquid, long-term bilateral contract market. Brito and Hartley show that there can be four different market structures in a stationary equilibrium:

(i) Firms search for a partner before investing and also search when in a poor match;

(ii) Firms search for a partner before investing but stay in a poor match;

(iii) Firms invest in infrastructure first and continue to search when in a poor match;

(iv) Firms invest in infrastructure first but stay in a poor match.

The second regime resembles the traditional LNG market and is the preferred outcome for the initially chosen parameter values. Brito and Hartley then show that a reduction in \(K\), an increase in the number of market entrants each year, and especially an increase in the probability of a

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\(^7\) In commenting on Canes and Norman (1984) and related papers, Masten and Crocker observed that risk sharing arguments “do not provide a practical basis upon which to evaluate observed contractual arrangements without knowledge of the relative risk preferences of the parties involved.” That does not mean, however, that risk-sharing considerations are irrelevant to the demand for long-term contracts.
good match (a parameter in their model), can make the third equilibrium, with maximum spot trading, preferable to the other three.

This paper explains how a small exogenous increase in spot market liquidity could stimulate additional spot market trading and thus increase the probability of finding good matches in the spot market. Simultaneously, the surplus from trading under a long-term contract would decline, thereby likely reducing the liquidity of the long-term bilateral contract market. Our results thus provide additional microeconomic foundations for the model examined by Brito and Hartley.

Nevertheless, the model in this paper need not predict the demise of long-term LNG contracts. A third alternative to traditional long-term contracts or trading only in a spot market is that long-term contracts become more flexible and allow partners to exploit more spot trading opportunities. Brito and Hartley ruled this possibility out by assumption. In their framework, firms trade with only one partner at a time. The long-term contracts we consider allow firms to complement contracted trade with spot market trades. Our results suggest that long-term LNG contracts will continue to evolve toward offering such increased flexibility.

4. A Model of long-term LNG contracts

The main reason for modeling the value of long-term contracts to firms trading LNG is to understand how potential increases in spot market liquidity may affect the nature or viability of long-term contracts. Thus, we assume that the alternative to a long-term contract is trading in a spot market. This contrasts with the models in Crocker and Masten (1988) or Ruester (2009), for example, which assume that absent a long-term contract the trading parties would engage in repeated costly bilateral bargaining.
Long-term contracts reduce cash flow volatility, which allows investments to be financed with more debt. On the other hand, they may lead to some trades that are ex-post inefficient. This happens even though, as emphasized by Masten and Crocker (1985) and others, a take-or-pay clause limits ex-post efficiency losses. Long-term contracts that allow spot transactions to complement contracted trade also have an option value. For example, when output is temporarily constrained or spot prices are low, exporters can fulfill their contract obligations by a swap, and when demand is low or spot market prices are high, importers can dispose of surplus contracted volume. The availability of such options reduces the ex-post inefficiency of contracts and helps make them more desirable. The optionality embedded in a contract also introduces substantial non-linearities that make the model impossible to solve analytically. We therefore use a numerical analysis of a stylized environment for trading LNG.\(^8\)

4.1 The investment projects

We obtain numerical values for the investments, volumes traded and prices that are representative for the LNG industry by using data on projects to cost a 5-mtpy liquefaction plant. LNG buyers will also often need to finance long-lived investments such as regasification terminals, storage facilities, pipelines, power plants and other industrial facilities. For our purpose, the aggregate cost of these investments is of most interest. To minimize the data that we need to gather and explain, we assume that no additional regasification, storage or pipeline capacity is needed and that all the natural gas will be used to fuel new CCGT power plants.

\(^8\) Even the numerical analysis was not straightforward. Search algorithms based on local derivatives of the objective often stopped at different solutions when using different starting values. The global pattern search algorithm in MatLab attained the same solution regardless of the choice of starting values, but converged slowly.
With approximately 51.322 mmbtu per tonne of LNG, a 5-mtpy plant would produce about 256.6×10^6 mmbtu/year of natural gas. Using EIA indicative data for CCGT plants, we assume each plant has 400MW capacity and a heat rate of 6.43 mmbtu/MWh. If the plants operate at an average 60% load factor, each plant would require 13.518×10^6 mmbtu/year of natural gas. Thus, eighteen CCGT power plants would consume approximately 243.33×10^6 mmbtu/year of natural gas. We aggregate the eighteen power plants into one importer facing the single exporter-owner of the liquefaction plant. We assume both the importer and the exporter maximize after-tax net present value of profits.

Using data on 24 liquefaction plants (culled from news reports) we related real costs (in billions of 2010 US dollars) to the natural log of plant capacity in mtpy. The relationship implies that a 5-mtpy plant would cost around $9.119 billion. Average real operating cost (excluding cost of feed gas) from the same plants was $0.28/mcf, which would give tax-deductible variable annual operating costs of around $0.2726 million per 10^6 mmbtu/year.

For the power plants, EIA data suggests a capital cost of $1.003 million/MW, implying that eighteen 400MW plants would cost $7.221 billion. Fixed operations and maintenance (O&M) costs of $0.01462 million/MW implies fixed O&M of $105.264 million per year for eighteen 400MW plants. Variable O&M (excluding fuel) of $3.11/MWh and a heat rate of 6.43 mmbtu/MWh imply annual non-fuel variable O&M of $0.4837 million/10^6 mmbtu.

Using data on almost 380 shipping routes, we found that, beyond about 3,000 miles, marginal shipping costs per mmbtu were well approximated by a linear function of distance. Assuming a representative distance of about 7,000 miles, we set shipping costs $S = $1.25/mmbtu.

\footnote{The 5\% difference from the liquefaction plant output would allow some LNG to be lost in transport.}
For simplicity, we assume linear demand and supply curves for LNG (this effectively assumes a linear supply curve for plant feed gas). Supply and demand are also affected by random shocks, $\xi$ and $\epsilon$, that cause parallel shifts in the curves. The demand shocks could result, for example, from plant outages, changes in other fuel prices or the prices of other inputs, or shocks to electricity demand. Supply shocks could result, for example, from plant outages, weather shocks, or strikes. In order to have “normal-looking” hump-shaped distributions with finite support, we assume that both shocks follow symmetric beta distributions with a coefficient of 3.25, but $\epsilon$ can shift the demand curve intercept by ±4 while $\xi$ can shift the supply curve intercept only by ±0.7. We also assume the values of $\epsilon$ and $\xi$ in any period are not public knowledge, and are too costly to verify to be made the subject of any contract.

In summary, we assume that the supply of LNG exports is given by

$$X^s = \frac{p_X - V_X - \delta - \xi}{\gamma}$$

(1)

where $p_X$ is the export netback price, $\delta = $1/mmbtu$^{10}$ and $\gamma = 0.035$, and demand for LNG is

$$M^D = \frac{\alpha + \epsilon - p_M - V_M}{\beta}$$

(2)

where $p_M$ is the landed price of LNG, $\alpha = $20/mmbtu and $\beta = 0.035$. Thus, at the mean intercept values, the maximum volume of trade (where the demand and supply prices differ by $S + V_X + V_M$) would be $242.768 \times 10^6$ mmbtu/year and the price to the importer would be $11.02$/mmbtu$^{11}$ (yielding a netback price to the exporter of $9.77$/mmbtu). The resulting outcome is represented in Figure 3. From the envelope theorem, we can interpret the area under

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$^{10}$ Note that a price measured as $$/mmbtu translates to an equivalent of millions of dollars per $10^6$ mmbtu so the units of $p$ in Figure 3 are millions of dollars.

$^{11}$ This approximates the National Balance Point (UK) and Japan-Korea Marker prices prior to them separating when the Fukushima disaster occurred.
the input demand curve between two prices $p_0$ and $p_1$ as the change in importer short-run profit from a change in input fuel price. Similarly, the area above the supply curve between two prices $p_0$ and $p_1$ is the change in exporter short-run profit from a change in output LNG price.

The parties can also trade in a spot market where prices vary randomly, but do not depend on trades by the two contracting parties. Denote the netback spot price available to the exporter by $p_X$ and the delivered spot price available to the importer by $p_M$. The destination for a spot cargo from the exporter, and the origin of a spot cargo delivered to the importer, are likely to vary from one transaction to the next. Thus, $p_X$ and $p_M$ should be positively, but not perfectly, correlated.

Specifically, we assume that $p_X$ can follow various symmetric beta distributions with a mean value of $8.75$ or $9.25$ and standard deviations ranging from $0.82$ to $1.41$, while

$$p_M = p_X + \nu$$

(3)

where $\nu$ also follows symmetric beta distributions independent of the distributions of $p_X$. If the spot market is well arbitraged, it would not be possible to buy LNG at $p_M$ pay $S = 1.25$/mmbtu to ship it to the exporter location and sell it at a profit for $p_X$. Thus, the standard deviations and means of $\nu$ are chosen to ensure $\nu = p_M - p_X > -S = -1.25$. In the examples, the mean of $\nu$ ranges from $1.9375$ to $3.25$, while the standard deviation ranges from $0.6162$ to $1.2324$. For these distributions, $\text{Pr}(\nu > S) = \text{Pr}(p_M > p_X + S)$ averages $0.8959$, with a minimum value of $0.7043$ and a maximum value of $1.00$. Hence, bilateral trade between the two parties is likely to be preferable to spot trades most of the time.

4.2 Financial parameters

We use the adjusted present value approach to value the two investment projects, assuming that the net benefit of debt can be approximated by its corporate tax benefits alone. The firm’s after-
tax cash flows, exclusive of tax benefits from depreciation allowances and interest payments, are discounted at the all-equity real rate of return of 10%. The corporate tax savings from debt are valued at the debt interest rate of \( r_B = 5\% \). The tax benefits resulting from the depreciation allowances are valued at the risk-free\(^{12} \) rate of interest of 3%. All projects have a 25-year life with straight-line depreciation. The corporate tax rate, \( \tau \), is 35%.

In addition, a “value at risk” type of constraint limits firm indebtedness.\(^{13} \) Denote the after-tax, but before interest, annual cash flow for particular values of demand (\( \varepsilon \)) and supply (\( \zeta \)) shocks, and export netback (\( p_X \)) and delivered import (\( p_M \)) spot prices by \( C(\varepsilon, \zeta, p_X, p_M) \). With debt \( B \) the after-tax annual interest cost is \( (1-\tau)r_B B \). We then require that the probability that \( C(\varepsilon, \zeta, p_X, p_M) \) is insufficient to cover the after-tax interest cost plus 10% of the principal be just 5%:

\[
\Pr\left[ C(\varepsilon, \zeta, p_X, p_M) < 0.1B + (1-\tau)r_B B \right] = 0.05
\]

4.3 Trading without a contract but under full information

We examine two scenarios where the parties trade without a contract. To establish a theoretically optimal level of ex-post trade between the parties, we first consider the unrealistic\(^{14} \) case where both parties know \( V_X, V_M, \zeta \) and \( \varepsilon \).

Define two “reference prices” for the exporter and importer such that supply equals demand and the prices differ by exactly the transport cost plus the sum of non-fuel variable costs, \( S+V_X+V_M \):

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\(^{12} \)The allowances are known for sure once the investment has been made.

\(^{13} \)As Weems (2006) notes, contracts began to include provisions aimed at “ensuring seller’s revenues were not unnecessarily interrupted” as project-financed liquefaction plants became more prevalent in the 1980s. While the specific form of the constraint we impose may not correspond well to the provisions that are used in practice, it does reflect the general idea that the cash flows associated with debt are non-contingent on market outcomes while those associated with equity are contingent. Hence, higher debt in the capital structure favors long-term contracts that help ensure at least part of the revenue stream is relatively constant.

\(^{14} \)If trades and prices depended on such information, parties would have an incentive to misrepresent the truth. It may also be impossible or costly for an outside party to verify the truth.
\[
\frac{\tilde{p}_X}{\tilde{p}_M} = \frac{\gamma(\alpha + \varepsilon - S - V_X - V_M) + \beta(\delta + \xi)}{\beta + \gamma}
\]

(5)

\[
\frac{\tilde{p}_M}{\tilde{p}_M} = \frac{\gamma(\alpha + \varepsilon) + \beta(\delta + \xi + S + V_X + V_M)}{\beta + \gamma}
\]

(6)

There are four possible outcomes depending on the current values of \(p_X\) and \(p_M\).

**Case 1: \(p_X + S \geq p_M\)**

Both the importer and the exporter prefer to use the spot markets. The resulting contributions to variable profits would be

\[
\Pi^v_M = \frac{(\alpha + \varepsilon - p_M - V_M)^2}{2\beta}
\]

\[
\Pi^v_X = \frac{\gamma(p_X - V_X - \delta - \xi)^2}{2\gamma}
\]

(7)  (8)

**Case 2: \(p_X + S < p_M\)**

The exporter prefers bilateral trade at \(p_M - S\) to spot trade at \(p_X\). There are three sub-cases.

**Case 2a: \(p_X - V_X \leq \tilde{p}_X\) and \(p_M + V_M \geq \tilde{p}_M\)**

Both the importer and the exporter prefer bilateral trade at prices (5) and (6) to spot trade. The resulting contributions to variable profits would be

\[
\Pi^v_M = \frac{(\alpha + \varepsilon - \tilde{p}_M)^2}{2\beta}
\]

\[
\Pi^v_X = \frac{(\tilde{p}_X - \delta - \xi)^2}{2\gamma}
\]

(9)  (10)

**Case 2b: \(p_X - V_X \leq \tilde{p}_X\) but \(p_M + V_M < \tilde{p}_M\)**

The importer only would prefer to trade spot. Since the spot market supply curve is perfectly elastic, \(p_M\) would set the terms for trade between the parties. The importer would pay \(p_M\), demand
as given by (2), and earn short-run profit (7). If the exporter wants to produce more than \( M^D \) at \( p_M-S \), any excess must be sold spot at \( p_X \). Maximum production at \( p_M-S \) is thus

\[
X_M^S = \min \left( \frac{p_M-S-V_X-\delta-\xi}{\gamma}, M^D \right)
\]

(11)

and spot market supply from the exporter, if any, would be

\[
X^S = \max \left( \frac{p_X-V_X-\delta-\xi}{\gamma} - X_M^S, 0 \right)
\]

(12)

The contribution to the short-run profit of the exporter in this case would be

\[
\Pi_X = \left( p_M-S-V_X-\delta-\xi \right) X_M^S + \left( p_X-V_X-\delta-\xi \gamma X_M^S \right) \frac{X^S}{2}
\]

(13)

Case 2c: \( p_X-V_X > \bar{p}_X \)

We need not consider \( p_M+V_M < \bar{p}_M \) since (recalling that here \( p_X+S < p_M \)) this would lead to

\[
\bar{p}_M > p_M+V_M > p_X+S+V_M > \bar{p}_X+S+V_X+V_M
\]

contradicting the definition of \( \bar{p}_X \) and \( \bar{p}_M \).

Thus, \( p_M+V_M \geq \bar{p}_M \), and we conclude that the importer would prefer to buy from the exporter.

Also, since \( p_X-V_X > \bar{p}_X \), the exporter will only trade for at least \( p_X \). Hence, regardless of where output is sold, the exporter would obtain \( p_X \). Exporter supply \( X^S \) would be given by (1) and the contribution to variable profits by (8). If the importer demands more than \( X^S \) at price \( p_X+S \) it will have to be bought spot. Product taken from the exporter would then satisfy

\[
M_X^D = \min \left( \frac{\alpha+\epsilon-p_X-S-V_M}{\beta}, X^S \right)
\]

(14)

and importer spot market purchases, if any, would be
\[ M^D = \max \left( \frac{\alpha + \epsilon - p_M - V_M}{\beta} - M^D_x, 0 \right) \] (15)

The contribution to importer short-run profit in this case would be

\[ \Pi'_M = \left( \alpha + \epsilon - p_X - S - V_M - \frac{\beta}{2} M^D_x \right) M^D_x + \left( \alpha + \epsilon - \beta M^D_x \right) \frac{M^D}{2} \] (16)

4.4 Trading without a contract and with public information only

We now make the more realistic assumption that trade in the absence of a contract must be based solely on \( p_X, p_M \) and \( S \). In the sequel, we will refer to this as the PI solution.

Define two reference prices that “split the difference” between \( p_M \) and \( p_X + S \):

\[ \hat{p}_X = \frac{p_M + p_X - S}{2} \] (17)

\[ \hat{p}_M = \frac{p_M + p_X + S}{2} \] (18)

along with the corresponding demand and supply at the prices (17) and (18) given by:

\[ \hat{M}^D = \frac{\alpha + \epsilon - \hat{p}_M - V_M}{\beta} \] (19)

\[ \hat{X}_S = \frac{\hat{p}_X - V_X - \delta - \xi}{\gamma} \] (20)

As in the full information world, we again have four cases.

**Case 1:** \( p_X + S \geq p_M \)

Both parties prefer to trade spot and (7) and (8) would give the contributions to short-run profits.

**Case 2:** \( p_M > p_X + S \)

Again there are three sub-cases, now depending on the relative values of \( \hat{M}^D \) and \( \hat{X}_S \).
Case 2a: $\hat{M}^D > \hat{X}^S$

The importer would need to satisfy any additional demand using the spot market, so

$$M^D = \max \left( \frac{\alpha + \epsilon - p_M - V_M}{\beta} - \hat{X}^S, 0 \right)$$  \hspace{1cm} (21)

The contributions to short-run profits would be

$$\Pi^\nu_M = \left( \alpha + \epsilon - \hat{p}_M - V_M - \beta \frac{\hat{X}^S}{2} \right) \hat{X}^S + \left( \alpha + \epsilon - \beta \hat{X}^S - p_M - V_M \right) \hat{M}^D$$  \hspace{1cm} (22)

$$\Pi^\nu_X = \frac{(\hat{p}_X - V_X - \delta - \xi) \hat{X}^S}{2}$$  \hspace{1cm} (23)

Case 2b: $\hat{M}^D < \hat{X}^S$

The exporter would need to dispose of any surplus supply using the spot market, so

$$X^S = \max \left( \frac{p_X - V_X - \delta - \xi}{\gamma} - \hat{M}^D, 0 \right)$$  \hspace{1cm} (24)

The contributions to short-run profits would be

$$\Pi^\nu_M = \frac{\left( \alpha + \epsilon - p_M - V_M \right) \hat{M}^D}{2}$$  \hspace{1cm} (25)

$$\Pi^\nu_X = \left( \hat{p}_X - V_X - \delta - \xi - \gamma \frac{\hat{M}^D}{2} \right) \hat{M}^D + \left( p_X - V_X - \delta - \xi - \gamma \hat{M}^D \right) \frac{X^S}{2}$$  \hspace{1cm} (26)

Case 2c: $\hat{M}^D = \hat{X}^S$

The contributions to short-run profits would be

$$\Pi^\nu_M = \frac{\left( \alpha + \epsilon - \hat{p}_M - V_M \right)^2}{2 \beta}$$  \hspace{1cm} (27)

$$\Pi^\nu_X = \frac{(\hat{p}_X - V_X - \delta - \xi)^2}{2 \gamma}$$  \hspace{1cm} (28)
4.5 Trading under a contract

Finally, we consider trading under a long-term contract with the following features. There is a contract price \( p \), yielding a netback price \( p-S \), for LNG delivered by the exporter to the importer. A volume \( q \) must be delivered unless both parties agree to a lesser amount. A take-or-pay clause requires the importer to compensate the exporter for any loss \( (p-S-p_X)(q-M) \equiv \phi(q-M) \) if the importer takes \( M < q \) when \( p_X < p-S \). Either party can supplement contracted trade with spot market transactions.\(^{15}\)

We assume \( p \) and \( q \) maximize the sum of the expected net present values of after-tax profits from the two investment projects. However, we also impose incentive compatibility constraints. The expected net present value of profits obtained by each party under the contract must be non-negative and at least as good as the expected net present value of the profits that party could obtain under the PI solution.

There are now five outcomes for spot and contracted trades for different values of \( p_X \) and \( p_M \).

Case 1: \( p_M \geq p_X+S \)

Here, we also have \( p_M+\phi = p_M+p-S-p_X \geq p \), so the importer would prefer to take the contracted supply at \( p \) than buy spot at \( p_M \) and pay \( \phi \). The exporter thus will supply \( q \) and may make additional spot market sales at price \( p_X \)

\[
X^S = \max \left( \frac{p_X-V_X-\delta-\xi}{\gamma} - q, 0 \right)
\]  
(29)

\(^{15}\) The theoretical contract examined here might allow the parties to engage in much more spot trading than actual contracts. If so, the strong performance of this contract relative to the theoretical first-best outcome suggests a possible avenue for increasing the flexibility of long-term contracts while maintaining their viability. Actual long-term contracts are confidential, but they must contain many details since, as Weems (2006) notes, their length has continued to increase in recent years with the longest contract he reviewed exceeding 175 pages.
The contribution of all the transactions to short-run exporter profit would be

$$\Pi_X^v = \left( p - S - V_x - \delta - \xi - \frac{\gamma q}{2} \right) q + \left( p_x - V_x - \delta - \xi - \gamma q \right) \frac{X^s}{2} \quad (30)$$

**Case 1a:** Importer demand at $p$ is strictly less than $q$.

The importer will sell the difference between the contracted amount and demand at $p_x$ and avoid incurring transport cost $S$. Such sales will be at a loss if $p_x < p - S$, but the loss would still be less than exercising the take-or-pay clause. The opportunity cost of LNG to the importer will therefore be $p_x + S$ and the importer will consume

$$M^D_X = \frac{\alpha + \epsilon - p_x - S - V_M}{\beta} \quad (31)$$

The contribution to importer short-run profits will be

$$\Pi_M^v = \left( \alpha + \epsilon - p - V_M - \beta \frac{M^D_X}{2} \right) M^D_X + \left( p_x + S - p \right) (q - M^D_X) \quad (32)$$

**Case 1b:** $M^D_X \geq q$

The importer may make additional spot purchases at price $p_M$

$$M^D = \max \left( \frac{\alpha + \epsilon - p_M - V_M - q}{\beta}, 0 \right) \quad (33)$$

and the resulting contribution of all transactions to short-run profits would be

$$\Pi_M^v = \left( \alpha + \epsilon - p - V_M - \frac{\beta q}{2} \right) q + \left( \alpha + \epsilon - \beta q - p_M - V_M \right) \frac{M^D}{2} \quad (34)$$

**Case 2:** $p_M < p_x + S$

We now have three sub-cases to consider.

**Case 2a:** $p_x + S > p$ and the importer wishes to purchase less than $q$ at price $p$
The exporter would agree to sell less than \( q \) to the importer at price \( p \). Furthermore, using a swap to fulfill the contract avoids the transport cost \( S \). The exporter thus purchases

\[
X^D = \min \left( \frac{\alpha + \epsilon - p - V_M}{\beta}, q \right)
\]  

(35)

spot at price \( p_M \) to make the swap. The exporter then independently makes spot sales at price \( p_X \) of amount

\[
X^S = \frac{p_X - V_X - \delta - \xi}{\gamma}
\]  

(36)

The contribution to exporter short-run profits in this case would be

\[
\Pi_X^* = (p - p_M)X^D + \frac{(p_X - V_X - \delta - \xi)^2}{2\gamma}
\]  

(37)

Case 2b: \( p_X + S > p \) and the importer wishes to purchase more than \( q \) at price \( p_M \)

Importer demand is now

\[
M^D = \max \left( \frac{\alpha + \epsilon - p_M - V_M}{\beta} - X^D, 0 \right)
\]  

(38)

The contributions to importer short-run profits would be

\[
\Pi_M^* = \left( \alpha + \epsilon - p - V_M - \beta \frac{X^D}{2} \right)X^D + \left( \alpha + \epsilon - \beta X^D - p_M - V_M \right)\frac{M^D}{2}
\]  

(39)

Case 2c: \( p_M < p_X + S \leq p \)

The importer exercises the take-or-pay clause and both parties use the spot markets. The contributions to short-run profits in this case will be

\[
\Pi_M^* = \frac{(\alpha + \epsilon - p_M - V_M)^2}{2\beta} - (p - S - p_X)q
\]  

(40)
5. Effects of changes in the market environment

Since we are interested in the effects of changes in the probability distributions of spot prices, we solved for $p$ and $q$ and a number of other variables of interest in the optimal contract and two non-contract solutions, for 75 different distributions for $p_X$ and $v$. Specifically, for each of two possible means ($8.75/\text{mmbtu}$ and $9.25/\text{mmbtu}$) for $p_X$ and three possible means ($1.9375/\text{mmbtu}$, $2.4375/\text{mmbtu}$ and $3.25/\text{mmbtu}$) for $v$, we calculated the solutions for a number of different variances of $p_X$ and $v$. For the full set of solutions, the contract price averaged $11.032/\text{mmbtu}$ with a standard deviation of $0.247/\text{mmbtu}$. The contract volume averaged $232 \times 10^6 \text{mmbtu/year}$, with a standard deviation of $5.6 \times 10^6 \text{mmbtu/year}$ and a range from $220.2 \text{–} 241.8 \times 10^6 \text{mmbtu/year}$.\textsuperscript{16}

5.1 Effects of changes in average spot prices

Table 1 summarizes how average values for $p$ and $q$ and other variables of interest vary as a function of the means of the spot price distributions. Uniformly increasing spot market prices (increasing $E(p_X)$ holding $E(v)$ fixed) by 50¢ raises the contract price by approximately 45¢ and the contract volume by about 4.5%. Since the supplier’s costs do not depend on the spot price, a uniform increase in spot prices benefits the supplier but also makes bilateral trade more desirable. Joint profits are maximized by trading a slight reduction in the average relative price

\[
\Pi_X^\gamma = \frac{(p_X - V_X - \delta - \xi)^2}{2\gamma} + (p - S - p_X)q
\]  \hspace{1cm} (41)

\textsuperscript{16} Recall that a 5 mtpy LNG plant would produce about $257 \times 10^6 \text{mmbtu/year}$, while eighteen 400MW CCGT power plants operated at 60% load factor would consume about $243 \times 10^6 \text{mmbtu/year}$. Since importer net spot market purchases average $28.6 \times 10^6 \text{mmbtu/year}$, the power plants on average operate at a higher than 60% load factor. Average exporter net spot market sales of $23.8 \times 10^6 \text{mmbtu/year}$ imply that the LNG plant would on average produce close to the rated $257 \times 10^6 \text{mmbtu/year}$.
\( p/E(p_X) \) for increased volume \( q \). However, the fact that the optimal contract price \( p \) rises by almost the full amount of the uniform change in spot prices is consistent with the observed almost full indexation of contract prices to shocks likely to have such a uniform effect.

Table 1: Average values of key variables by spot price distribution means\(^a\)

<table>
<thead>
<tr>
<th>( E(p_X) )</th>
<th>( E(v) = E(p_M) - E(p_X) )</th>
<th>8.75</th>
<th>9.25</th>
</tr>
</thead>
<tbody>
<tr>
<td>Number of distributions</td>
<td>12</td>
<td>15</td>
<td>15</td>
</tr>
<tr>
<td>Contract price ( p ) ($/mmBtu)</td>
<td>10.68</td>
<td>10.97</td>
<td>10.90</td>
</tr>
<tr>
<td>Contract quantity ( q ) (10(^6) mmBtu/year)</td>
<td>223.09</td>
<td>229.59</td>
<td>230.90</td>
</tr>
<tr>
<td>( E(NPV_X) ) under contract ($ m)</td>
<td>45.10</td>
<td>487.06</td>
<td>463.35</td>
</tr>
<tr>
<td>( E(NPV_M) ) full information ($ m)</td>
<td>2.4375</td>
<td>3.25</td>
<td>1.9375</td>
</tr>
<tr>
<td>( E(NPV_X) ) public information ($ m)</td>
<td>1547.12</td>
<td>230.90</td>
<td>1233.85</td>
</tr>
<tr>
<td>( E(NPV_M) ) full information ($ m)</td>
<td>1662.83</td>
<td>1121.91</td>
<td>1352.58</td>
</tr>
<tr>
<td>( E(NPV_M) ) public information ($ m)</td>
<td>1533.69</td>
<td>792.61</td>
<td>1205.90</td>
</tr>
<tr>
<td>Debt ( B_X ) under contract ($ m)</td>
<td>5176.72</td>
<td>5490.05</td>
<td>5430.67</td>
</tr>
<tr>
<td>Debt ( B_X ) full information ($ m)</td>
<td>3827.87</td>
<td>4435.16</td>
<td>4135.53</td>
</tr>
<tr>
<td>Debt ( B_X ) public information ($ m)</td>
<td>3612.66</td>
<td>4016.04</td>
<td>3997.10</td>
</tr>
<tr>
<td>Debt ( B_M ) under contract ($ m)</td>
<td>3162.26</td>
<td>2785.63</td>
<td>2966.36</td>
</tr>
<tr>
<td>Debt ( B_M ) full information ($ m)</td>
<td>3277.38</td>
<td>3292.48</td>
<td>2917.39</td>
</tr>
<tr>
<td>Debt ( B_M ) public information ($ m)</td>
<td>2620.52</td>
<td>2350.06</td>
<td>2500.51</td>
</tr>
<tr>
<td>Contract premium relative to PI</td>
<td>30.97%</td>
<td>34.26%</td>
<td>26.54%</td>
</tr>
<tr>
<td>Importer spot net purchases</td>
<td>50.12</td>
<td>15.96</td>
<td>53.34</td>
</tr>
<tr>
<td>Exporter spot net sales</td>
<td>28.48</td>
<td>9.83</td>
<td>42.86</td>
</tr>
</tbody>
</table>

\(^a\) There were no feasible solutions for \( p \) and \( q \) when \( E(p_X)=8.75 \) and \( E(v)=1.9375 \) since bilateral trade between the exporter and importer is uncompetitive at such low spot prices. When \( E(p_X)=8.75 \) and \( E(v)=2.4375 \) there also were no feasible solutions for low values for the variances of \( p_X \) and \( v \).

An increase of 50¢ in the spread \( E(v) \), which corresponds to a decrease in competition for the exporter, raises the contract price by about 20¢ on average and the contract volume by about 1.8%. These are less than half the corresponding effects of an increase in \( E(p_X) \) holding \( E(v) \) fixed. When spot prices available to the importer alone rise, the opportunity cost for the exporter of trading with the importer is unchanged so the increase in contract price is less.

Strictly positive expected net present values imply that the expected returns on the investments exceed the required rates used to discount the cash flow components. For the exporter, \( E(NPV_X) \) under the contract solutions range from around 0.5% to almost 14% of the up-front investment.
cost of $9,119 million. For the importer, $E(NPV_M)$ under the contract solutions range from around 1.9% to more than 21% of the up-front investment costs of $7,221 million.

A uniform increase in spot prices (an increase in $E(p_X)$ holding $E(v)$ fixed), or an increase in the average gap $E(v)$ (holding $E(p_X)$ fixed), increases $E(NPV_X)$ and reduces $E(NPV_M)$ in the contract solutions. Again the magnitude of the effect is smaller for the second type of change.

While the incentive compatibility constraint required only that the contract solution be at least as good as the $PI$ solution, $E(NPV_X)$ and $E(NPV_M)$ are in fact strictly larger under the optimal contract solutions. Average combined surplus, $E(NPV_X) + E(NPV_M)$, ranges from 26.54% to more than 34.26% above the corresponding $PI$ solutions.\(^\text{17}\) A smaller $E(v)$ between average spot prices reduces the advantages of a contract. A smaller gap implies that the pairing is less valuable relative to the alternatives.

Average exporter debt under the contract solution ranges from one-third to more than 43% higher than debt under the $PI$ solutions. The corresponding percentage differences for the importer range from 16–20% higher.\(^\text{18}\) As hypothesized, the tendency for the contract to stabilize cash flows allows the investing parties to carry more debt.

Higher debt under the contract solutions would increase expected net present values simply because of the assumed tax benefits of debt. However, these implied differences exceed the actual differences in expected net present values. Thus, the contract solutions impose ex-post trading losses that partially offset the gains from extra debt.

\(^{17}\) Average $E(NPV_X)$ in the no-contract solutions is negative when $E(p_X)=8.75$ and $E(v)=2.4375$ so average spot prices are very low. In these cases, bilateral trade would not occur without a contract.

\(^{18}\) The sum of the debt carried by the exporter and the importer is also always higher under the contract solution than under the full information no-contract solutions. However, the importer typically carries more debt under the full information solutions than under the contract solutions.
The final two rows show that both importer spot market net purchases and exporter spot market net sales increase substantially as the average gap $E(v)$ decreases. With a smaller gap, the probability that $p_M < p$ and the probability that $p_X > p-S$ both increase, raising the value of the embedded options to trade on spot markets. An increase in $E(p_X)$ holding $E(v)$ fixed increases exporter net spot sales and decreases importer net spot purchases.\(^{19}\)

5.2 Effects of changes in the variability of spot prices

We summarized the effects of changes in variances by estimating and plotting a set of regression surfaces.\(^{20}\) For each pair of values for $E(p_X)$ and $E(v)$, the solutions for $p$ and $q$ and other outcomes of interest are non-linear functions of the standard deviations $\sigma(p_X)$ and $\sigma(v)$. Each non-linear function can be approximated by a polynomial expansion, which is then used to interpolate and plot values for the outcome of interest for other values of $\sigma(p_X)$ and $\sigma(v)$. In practice, we required a cubic polynomial to reasonably approximate the solution values.\(^{21}\)

Figure 4 graphs the approximate solution for the optimal contract price $p$ as a function of $\sigma(p_X)$ and $\sigma(v)$ and for the different values of $E(p_X)$ and $E(v)$.\(^{22}\) The effects of $\sigma(p_X)$ and $\sigma(v)$ on $p$ are, at their largest, similar in magnitude to the effects of $E(v)$, but in several cases the changes in $p$ are much smaller. Figure 5 graphs the corresponding solutions for optimal contract volume $q$. The highly non-linear effects of spot price variances on $p$ and $q$ (and some other variables of interest) may be because the embedded options to exploit spot trades, and the values of any efficient ex-

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\(^{19}\) While average exporter net spot sales are smaller when $E(p_X)=9.25$ and $E(v)=2.4375$ than when $E(p_X)=8.75$ and $E(v)=2.4375$, the solutions in the former case include an extra six cases with low variances. Restricting calculations to cases where variances are identical, average exporter net spot sales when $E(p_X)=9.25$ and $E(v)=2.4375$ are 31.07.

\(^{20}\) The solution values underlying the figures plotted in the paper are available from the author on request.

\(^{21}\) We also fit cubic spline interpolations, which match the solution values exactly. These looked quite similar to the figures in the paper, but were less smooth since the coefficients vary with $\sigma(p_X)$ and $\sigma(v)$.

\(^{22}\) Since an increase in $p$ redistributes rents from importer to exporter, graphs of the share of rent accruing to the exporter (not included in the paper) look quite similar to the graphs of the optimal contract price $p$. 

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post trades precluded by the contract, are both affected non-linearly by changes in $\sigma(p_X)$ and $\sigma(\nu)$.

Figure 6 graphs the ex-post spot market trading loss under the contract as a proportion of the sum of expected net present values under the full information solution. The loss is defined as the present value of the reduced tax benefits from debt under the full information solution minus the actual difference in the sum of expected net present values under the contract and the corresponding full information solution. From Figures 5 and 6, trading inefficiencies tend to be relatively low where contract volumes are relatively high and vice versa. When ex-post trading inefficiencies could be high, lower contract volumes leave contracting parties to rely more upon ex-post profitable spot trading opportunities.

Figure 7 provides more insight into spot trading under the optimal contracts. The values approximated in Figure 7 are ratios to optimal contract volume $q$ of summed expected spot market sales and purchases by either the exporter or the importer.\(^{23}\) Figure 7 shows that reduced variability of the gap $\sigma(\nu)$ decreases spot market transactions, probably because it reduces the value of the embedded options. Reducing $\sigma(p_X)$ also tends to decrease net spot market transactions, but the effect is much weaker. For $E(p_X)=9.25$ and $E(\nu)=1.9375$, as $\sigma(\nu)$ approaches the boundary of the region where $\Pr(p_M+S \leq p_X) > 0$ the total volume of spot market transactions from either party to the contract can exceed 75% of the contracted volume.

Figure 8 graphs the additional debt under the contract relative to the $PI$ solutions.\(^{24}\) This is not very sensitive to changes in $E(p_X)$ and $E(\nu)$ and, since the contours are close to vertical lines,

\(^{23}\) The graphs of spot net sales by the exporter looked very similar to Figure 7, while spot net purchases by the importer looked like the graphs in Figure 7 slightly rotated in the counter-clockwise direction. For $E(p_X)=9.25$, $E(\nu)=3.25$, the importer spot net purchases graph was also translated to the right.

\(^{24}\) The contract solutions also allow extra debt relative to the full information, but the difference is less.
changes in $\sigma(p_X)$ have a much stronger effect than changes in $\sigma(\nu)$. The sensitivity of additional debt to $\sigma(p_X)$ is consistent with the hypothesis that the contract stabilizes cash flows.

Figure 9 graphs the proportional increase in $E(NPV_X + NPV_M)$ under the contract relative to the PI solutions. The graphs in Figures 8 and 9 are quite similar, and much more linear than in Figures 4–7. While changes in spot price variances have complicated effects on spot market trading opportunities, non-linear changes in $p$ and $q$ evidently allow cash flows to change much more linearly in response to changes in $\sigma(p_X)$ and $\sigma(\nu)$. As a result, the additional debt afforded by a contract also changes more linearly.\(^{25}\)

The contract solution yields on average around 30% higher surplus than the corresponding PI solution.\(^{26}\) The advantage of a contract is not much affected by the general level $E(p_X)$ of spot market prices, but reducing the average gap $E(\nu)$ between $p_M$ and $p_X$ noticeably reduces the benefits of a contract. Figure 9 also reveals that a decrease in $\sigma(p_X)$ substantially reduces the benefits of a contract, but the effect of $\sigma(\nu)$ is weak and generally more ambiguous. Comparing Figures 8 and 9, the key reason for reduced benefits of a contract as $\sigma(p_X)$ declines is that reduced variability of spot prices also reduces the extra debt under a contract.

5.3 Effects of increasing spot market liquidity

The volume of LNG spot trading has been increasing, as have the numbers of participating buyers and sellers. In consequence, prices for spot trades have become less sensitive to individual trades. Entry by new suppliers and demanders also reduces the average distance between any two potential trading partners. This will in turn tend to reduce the gap between

\(^{25}\) The cubic approximations in Figures 8 and 9 also fit the calculated values much more accurately.

\(^{26}\) Because of differences in debt, $E(NPV_X + NPV_M)$ under the contract solutions is also approximately 12% higher on average than $E(NPV_X + NPV_M)$ under the corresponding full information solutions.
average spot prices available to exporters and importers, characterized as $E(\nu)$ in the model.

Increased liquidity should also reduce the variability of spot prices, denoted $\sigma(p_{X})$ in the model.

Reducing both $\sigma(p_{X})$ and $E(\nu)$ should reduce the superiority of long-term contracts relative to spot trading. At the same time, reducing $E(\nu)$ should greatly increase the amount of spot market trading from parties to existing contracts. Although a simultaneous reduction in $\sigma(\nu)$ would tend to have the opposite effect, the results in Figure 7 suggest that the change in $E(\nu)$ is likely to dominate. Overall, we therefore would expect spot trading volume to continue to grow relative to long-term contract volume.

The evolution of the US natural gas market after 1985, when the Federal Energy Regulatory Commission (FERC) allowed interstate natural gas pipelines to carry gas for their customers as contract carriers, may provide a precedent for how LNG markets could evolve. As noted by De Vany and Walls (1993), for example, prior to FERC Order 436 the requirement that pipelines buy and sell gas through long-term contracts precluded the development of spot markets for natural gas. De Vany and Walls noted that, despite deregulation, there were many reasons why arbitrage might not have been effective. Nevertheless, they present evidence that by 1987-88, 46% of the pairs of market prices that they examined were cointegrated,\(^{27}\) rising to 54% in 1988-89, 65% in 1989-90 and 66% in 1990-91. They also show that by the end of their sample in 1991 “the degree of cointegration between distant market-pairs approaches the cointegration of near pairs.” Furthermore, discontinuities in the pattern of cointegration matched the dates various pipelines were opened for access. Although there appeared to be many barriers to market integration, opening access allowed arbitrage and spot trading to develop rapidly.

\(^{27}\) As De Vany and Walls observe: “If two price series are within stable arbitrage limits, the ‘spread’ between them will be stationary and they will be cointegrated. Cointegration, therefore, is the natural test for market integration of stochastically varying prices.”
6. Concluding comments

As more firms import LNG, and more producers enter the market, the average difference between spot market prices available to an importer and netback prices available to an exporter will decline. The overall elasticity of supply or demand facing any one party also will increase. The use of natural gas in a wider range of applications may also raise demand elasticities. At the same time, more firms are positioning themselves to take advantage of geographic and intertemporal LNG price differentials. As a result of these developments, spot market prices are likely to become less variable.

The model presented in this paper suggests that these developments will erode the advantages of long-term contracts in allowing higher project leverage. At the same time, the changes are likely to increase spot market participation by parties under contract, further raising spot market liquidity. An increased desire to take advantage of spot and short-term arbitrage opportunities should also raise the demand for greater flexibility in long-term contracts. Accordingly, we can foresee continuing evolution of world LNG markets toward a larger proportion of volumes being traded on short-term contracts or sold as spot cargoes, and increased use of swaps, re-exports and other similar short-term arrangements taking advantage of temporary arbitrage opportunities.

7. References


Figure 1: Total, contracted and spot and short-term LNG trade by destination basin
Figure 2: US LNG imports by month

Figure 3: Trade between the exporter and importer
Figure 4: Approximate contract prices ($/mmbtu)

Figure 5: Approximate contract volumes ($10^6$ mmbtu/year)
Figure 6: Ex-post trading inefficiencies relative to the full information solution

Figure 7: Gross spot market transactions relative to contracted volumes
Figure 8: Additional exporter plus importer debt under the contract solutions

Figure 9: Contract solution premiums relative to the public information equilibriums